

How does the placement of steel in a composite beam affect its performance?

I-beams optimise material usage by positioning large flanges far from the neutral axis and connecting them with a relatively thin web. Similarly, PLX20 beams employ this concept to maximise the effectiveness of steel reinforcements, thereby significantly increasing bending stiffness. In PLX20 beams, the steel bars serve a similar function to the flanges of an I-beam, while the timber acts as the web.



Bending stiffness, aka flexural rigidity, is directly related to the second moment of inertia I of a beam's cross-section.

The second moment of inertia for a rectangular beam is calculated using this equation

$$I = \frac{bh^3}{12} + Ad^2$$

where

b is the width of the beam

h is the depth of the beam

A is the area of the beam equal to $b \times h$

d is the distance between the geometric centre and neutral axis (for a rectangular beam, the geometric centre and neutral axis are the same location, so this distance is zero)

Consider a 300×10 rectangular section bending about its major (strong) axis X-X. This means

$$b = 10$$

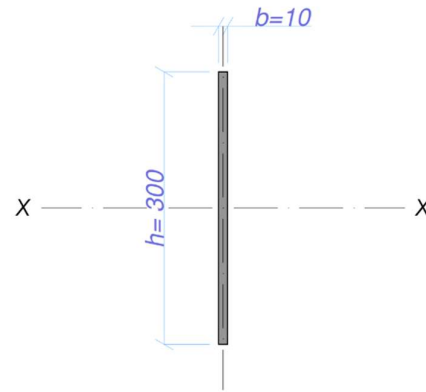
$$h = 300$$

$$A = 10 \times 300 = 3000$$

$$d = 0$$

The second moment of inertia for this beam is

$$I = \frac{bh^3}{12} + Ad^2 = \frac{10 \times 300^3}{12} + 3000 \times 0^2 = 22.5 \times 10^6$$



Now imagine the same rectangular section is broken into two pieces and placed 300 apart from each other. For each piece in the new configuration, it means

$$b = 150$$

$$h = 10$$

$$A = 10 \times 150 = 1500$$

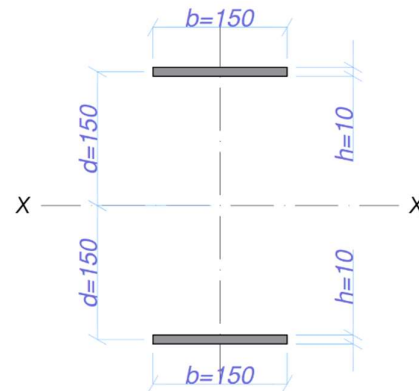
$d=150$ (geometric centre for each piece is 150 from the neutral axis, which has a significant impact on the second moment of inertia)

The second moment of inertia for each piece is

$$I = \frac{bh^3}{12} + Ad^2 = \frac{150 \times 10^3}{12} + 1500 \times 150^2 = 33.8 \times 10^6$$

The total second moment of inertia for both pieces is

$$2 \times (33.8 \times 10^6) = 67.5 \times 10^6$$



Comparing the second moment of inertia for two configurations

$$\frac{67.5 \times 10^6}{22.5 \times 10^6} = 3.0$$

This means, in this example, the second configuration has **three** times the bending stiffness while using the same amount of material.